

School of Civil & Environmental Engineering, Research Centre for Integrated Transport Innovation (rCITI)

**Pre-disaster Self-evacuation Transport Network Design under Uncertain Demand and Connectivity Reliability: A Novel Bilevel Programming Model**



Speaker: Junxiang Xu

Ph.D Candidate (T3, 2022)

Primary Supervisor: Divya Jayakumar Nair

Joint Supervisor: Milad Haghani

Secondary Supervisor: Steven Travis Waller

#### **Evacuation and self-evacuation**









Scenarios of the evacuation process over time



Scenarios of the self-evacuation process over time



## **Evacuation and self-evacuation**



Pre-disaster self-evacuation process diagram



## **Evacuation and self-evacuation**





## **1. Background and motivation**



Remote Sensing Imagery of Flood Disasters in the Greater Sydney Area **(03/2022)**

Remote Sensing Imagery of Flood Disasters in the Greater Sydney Area **(07/2022)**

Remote Sensing Imagery of Flood Disasters in the Greater Sydney Area **(09/2022)**

- Focus on the self-evacuation process and design a pre-disaster transport network with high efficiency.
- (2) Develop a novel bi-level programming model to solve network design problems under uncertain factors.
- (3) Innovate an improved user equilibrium, considering the psychological behavior of evacuees.



#### **2. Literature review**







Basic topology diagram of Self-evacuation transport network design (S-ETNDP)



# **4. Modeling characteristics**

- $\triangleright$  Disaster features
- $\triangleright$  Topological features
- $\triangleright$  Transport modes
- $\triangleright$  Evacuation features
- $\triangleright$  Evacuation target
- $\triangleright$  Budget cost
- $\triangleright$  Self-evacuation behavior









(2) **Highlight 1:** Quantifying network connectivity reliability based on percolation theory



(3) **Highlight 2:** Proposing a regret-risk utility function to describe the equilibrium conditions for the lower-level model



Upper-level model of S-ETNDP:

$$
\min Z_1 = \sum_{z \in S} X_z T_z (X_z)^* = \sum_{z \in S} X_z \cdot t_z^0 \cdot \left[ 1 + \alpha_z^0 \cdot \left( \frac{X_z}{C_z \cdot (1 - \theta_z)} \right)^0 \right] \tag{1}
$$

$$
\max Z_2 = \sum_{r=1}^{R} \prod_{rs} \left[ P\left( pt_i | k_i \right) \cdot P\left( pt_j | k_j \right) \right] r_s, \forall i, j \in N
$$
 (2)

Subject to:

$$
P(p t_i | \dot{x}_i) = \frac{1}{\sqrt{2\pi}\sigma(\dot{x}_i)} \cdot \exp\left[-\left(p t_i - \mu(\dot{x}_i)\right)^2 / \left(2\sigma(\dot{x}_i)^2\right)\right] = \frac{1}{\sqrt{2\pi}\sigma(\dot{x}_i)} \cdot \exp\left[-\left(\frac{\dot{x}_i}{a} - \mu(\dot{x}_i)\right)^2 / \left(2\sigma(\dot{x}_i)^2\right)\right], \forall i, j \in N
$$
\n(3)\n
$$
P(p t_j | \dot{x}_j) = \frac{1}{\sqrt{2\pi}\sigma(\dot{x}_j)} \cdot \exp\left[-\left(p t_j - \mu(\dot{x}_j)\right)^2 / \left(2\sigma(\dot{x}_j)^2\right)\right] = \frac{1}{\sqrt{2\pi}\sigma(\dot{x}_j)} \cdot \exp\left[-\left(\frac{\dot{x}_i}{a} - \mu(\dot{x}_j)\right)^2 / \left(2\sigma(\dot{x}_j)^2\right)\right], \forall i, j \in N
$$

$$
\sum\nolimits_{j\in N}{{\nu }_{j}}=m
$$

- $\sum_{s,s} z_s Y_s D_s \leq B$
- $0 \leq X_{1} \leq C_{1}$ ,  $\forall s \in S$  $(7)$
- $\tau_{cr} \in \{0,1\}$ ,  $\forall s \in S, r \in R$  $(8)$ 
	- $v_j \in \{0,1\}$ ,  $\forall j \in N$  $(9)$
- $Y_{1} \in \{0,1\}$ ,  $\forall s \in S$  $(10)$
- The objective function (1) of the upper-level model and represents the minimized total evacuation time in the self-evacuation network.
- The objective function (2) of the upper-level model represents the maximized network connectivity reliability.

(3) and (4) represent the expressions of the node percolation threshold probability functions.

Ensure that a certain number of shelters are selected.

Represents the constraint of the total investment budget for the self-evacuation transport network.

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 $(4)$  $(5)$ 

 $(6)$ 



Lower-level model of S-ETNDP:

 $\max Z_3 = \sum_{s \in S} \int_0^{X_s} \left\{ \frac{1 - \exp\left[\lambda \cdot T_s(X_s)^* \right]}{\lambda} + \frac{1 - \exp\left[\eta \cdot \left(T_s(X_s)^* - T_s(X_s)_{\min}^* \right) \right]}{\eta} \right\} dX_s$ 

Subject to:

$$
f_r^{\omega} = d^{\omega} \cdot \left\{ \frac{\exp\left\{1 - \exp\left[\lambda \cdot T_r\left(f_r^{\omega}\right)\right] + \frac{1 - \exp\left[\eta \cdot \left(T_r\left(f_r^{\omega}\right) - T_r\left(f_r^{\omega}\right)_{\min}\right)\right]\right\}}{\lambda}\right\}}{\sum_{i \in \mathcal{R}} \exp\left\{\frac{1 - \exp\left[\lambda \cdot T_i\left(f_i^{\omega}\right)\right] + \frac{1 - \exp\left[\eta \cdot \left(T_i\left(f_r^{\omega}\right) - T_i\left(f_r^{\omega}\right)_{\min}\right)\right]\right\}}{\eta}\right\}}
$$

$$
d^{\omega} = \sum_{r \in R} f_r^{\omega}
$$

$$
X_{\mathbf{s}} = \sum_{\omega} \sum_{r \in \mathbf{R}} f_r^{\omega} \cdot \tau_{\omega}, \forall s \in \mathbf{S}, \tau_{\mathbf{s}r} \in \{0,1\}
$$

$$
\sum\nolimits_{r\in R}f_r^{\omega}\leq \sum\nolimits_{j\in N}g_jv_j, \forall j\in N, v_j\in\left\{0,1\right\}
$$

$$
f_r^{\varpi} \geq 0, \forall r,l \in R, 0 < \lambda < 1, 0 < \eta < 1
$$

$$
T_r(f_r^{\omega}) = \sum_{s \in S} T_s(X_s)^* \tau_s, T_s(X_s)^* = t_s^0 \cdot \left[1 + \alpha_s^0 \cdot \left(\frac{X_s}{C_s \cdot (1 - \mathcal{G}_s)}\right)^{\beta}\right], \forall s \in S, r \in R
$$

 $(11)$ The objective function of the lower-level model.

- $(12)$ A traffic equilibrium condition based on the Regret-risk function.
- Represents the equilibrium relationship between demand and route flow in  $(13)$ the self-evacuation network.
- $(14)$ Represents the equilibrium relationship between road flow and route flow.
- The shelter capacity constraint  $(15)$
- $(16)$
- $(17)$ The basic road impedance and route impedance function definition.



#### Robust Optimization Approach—Just show the results

Upper-level model:

$$
\min Z_1 = \sum_{s \in S} X_s T_s (X_s)^* = \sum_{s \in S} \left( X_{s0} + \overline{X_s} \left\| s^{\alpha} \right\| \right) \cdot t_s^0 \cdot \left[ 1 + \alpha_s^0 \cdot \left( \frac{\left( X_{s0} + \overline{X_s} \left\| s^{\alpha} \right\| \right)}{C_s \cdot (1 - \theta_s)} \right)^{\beta} \right] \tag{70}
$$

$$
\text{ax}\,Z_2 = \sum_{r=1}^{R} \prod_{r=1} \left[ P\left( pt_i | k_i \right) \cdot P\left( pt_j | k_j \right) \right] r_r, \forall i, j \in N \tag{71}
$$

Subject to:

$$
\sum_{j \in N} \nu_j = m \tag{72}
$$

$$
\sum_{z \in S} z_z Y_z D_z \le B \tag{73}
$$

$$
\frac{\partial \left( X_{x0} + \overline{X}_z \middle\| s^a \right)}{\partial \left( d_0^a + \overline{d}^a \middle\| s^a \right)} + 2\overline{\alpha_1} \left( \frac{\overline{d}^a \middle\| s^a \right)}{d_0^a + \overline{d}^a \left\| s^a \right\|} \right) = 0, \forall s \in S
$$
\n(74)

$$
\varpi_{1}\left[1-\sum_{\omega}\left(\frac{\overline{d^{\omega}}\left\|\mathfrak{s}^{\omega}\right\|}{d_{\omega}^{\omega}+\overline{d^{\omega}}\left\|\mathfrak{s}^{\omega}\right\|}\right)^{2}\right]=0
$$
\n(75)

$$
\frac{\partial \left( X_{s0} + \overline{X}_s \left\| \mathbf{s}^c \right\| \right)}{\partial \left( d_0^{\sigma} + \overline{d^{\sigma}} \left\| \mathbf{s}^c \right\| \right)} - \frac{\partial C_s}{\partial \left( d_0^{\sigma} + \overline{d^{\sigma}} \left\| \mathbf{s}^c \right\| \right)} + 2\varpi_2 \left( \frac{\overline{d^{\sigma}} \left\| \mathbf{s}^c \right\|}{d_0^{\sigma} + \overline{d^{\sigma}} \left\| \mathbf{s}^c \right\| \right) = 0, \forall s \in S
$$
\n(76)

 $\overline{\omega}_1, \overline{\omega}_2 \geq 0$ 

$$
\varpi_2 \left[ 1 - \sum_{\alpha} \left( \frac{\overline{d^{\alpha}} \left\| s^{\alpha} \right\|}{d^{\alpha}_{\theta} + \overline{d^{\alpha}} \left\| s^{\alpha} \right\|} \right)^2 \right] = 0 \tag{77}
$$

$$
\tau_{rr} \in \{0, 1\}, \forall s \in S, r \in R
$$
\n
$$
(78)
$$

$$
\nu_{j}\in\left\{ 0,1\right\} ,\forall j\in N\tag{79}
$$

$$
Y_{s} \in \{0,1\}, \forall s \in S
$$
 (80)

Lower-level model:  
\n
$$
\max Z_{i} = \sum_{a \in I} \int_{0}^{x_{c}} \left[ \frac{1 - \exp\left[ \lambda \cdot T_{c}(X, Y^{*}) \right]_{0}^{2} + \exp\left[ \eta \cdot (T_{c}(X, Y^{*}) - T_{c}(X, Y^{*}) \right]_{0}^{2}}{\eta} \right] dX,
$$
\n(82)  
\n
$$
\theta \left[ \left( d_{\alpha}^{m} + \overline{d}^{m} \left\| \mathbf{r}^{m} \right\| \right) \cdot \left[ \frac{\exp\left[ \lambda \cdot T_{c}(X^{*}) \right]_{0}^{2} + \frac{1 - \exp\left[ \eta \cdot (T_{c}(X^{*}) - T_{c}(X^{*}) \right]_{0}^{2}}{\eta} \right] \right]}{\lambda^{2}} \right]
$$
\n
$$
+2\varpi_{0} \left( \frac{\overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2}}{\alpha_{0}^{m} + \overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2}} = 0, \forall r \in \mathbb{R}, d^{m} \in \mathcal{Q}
$$
\n
$$
\varpi_{1} \left[ 1 - \sum_{a \in I} \left( \frac{\overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2}}{\alpha_{0}^{m} + \overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2}} \right] \right] = 0
$$
\n
$$
\sum_{r \in I} \theta \left( d_{\alpha}^{m} + \overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2} \right) = 0
$$
\n(84)  
\n
$$
\sum_{r \in I} \theta \left( d_{\alpha}^{m} + \overline{d}^{m} \left\| \mathbf{r}^{m} \right\| \right) + 2\varpi_{c} \left( \frac{\overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2}}{\alpha_{0}^{m} + \overline{d}^{m} \left\| \mathbf{r}^{m} \right\|_{0}^{2}} \right) = 1, d^{m} \in Q, f^{m} \in \mathcal{Q}
$$

$$
T_{\epsilon}(X_{\epsilon})^* = t_{\epsilon}^{\theta} \cdot \left[1 + \alpha_{\epsilon}^{\theta} \cdot \left(\frac{X_{\epsilon \theta} + \overline{X_{\epsilon}} \left\| \epsilon^{\alpha} \right\|}{C_{\epsilon} \cdot (1 - \theta_{\epsilon})}\right)^{\theta}\right], T_{\epsilon}(f_{\epsilon}^{\theta \theta}) = \sum_{\epsilon \in \mathbb{N}} \left\{t_{\epsilon}^{\theta} \cdot \left[1 + \alpha_{\epsilon}^{\theta} \cdot \left(\frac{X_{\epsilon \theta} + \overline{X_{\epsilon}} \left\| \epsilon^{\alpha} \right\|}{C_{\epsilon} \cdot (1 - \theta_{\epsilon})}\right)^{\theta}\right], \tau_{\epsilon \theta}\right\}, \forall \epsilon \in S, r \in \mathbb{R}
$$
(92)

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 $(81)$ 



#### **6. Algorithm design: IGA-NSGA-II**





**7. Test network and case analysis**





Nguyen-Dupuis network Case study (Central Coast area of Greater Sydney, Australia)



#### **8. Research insights from N-D test network**



Exploring the changes in risk aversion and regret aversion parameters on the route choice utility.

Exploring the changes in risk aversion and regret aversion parameters on the road traffic flow.

Exploring the changes in risk aversion and regret aversion parameters on the route traffic flow.

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 $(0.04.0.08)$ 

 $(0.04, 0.10)$ 

9  $10$ 

#### **9. Research insights from case analysis network**





Design of a pre-flood self-evacuation transport network for the Central Coast region of New South Wales, Australia

The lower-level model traffic equilibrium process during IGA-NSGA- II execution



#### ◆ Research contributions

(1) A novel bi-level nonlinear programming model is developed to solve the self-evacuation transport network design problem under flood attacks.

(2) An approach to quantifying the uncertain connectivity reliability based on percolation theory is proposed, and a robust optimization approach is used to transform the bi-level model with uncertain demand.

(3) The model and algorithm in this paper can be applied to a real network of a certain size to give a solution that can directly answer the question of the potential equipped road construction option that should be chosen by the government authorities.

(4) The values of the risk aversion parameter and regret aversion parameter are proved to have a great influence on the model solution, where the risk aversion parameter has a greater impact on the total network utility value and both parameters have almost the same impact on the route traffic flow in the equilibrium period.

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#### **Junxiang Xu**

**Ph.D Candidate (T3, 2022)**



**UNSW Research Centre for Integrated Transport Innovation** 



[junxiang.xu@unsw.edu.au](mailto:junxiang.xu@unsw.edu.au)

THANK YOU

